



Solid state physics (*winter term 2015/2016*)

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Exercise sheet 1: Operation with vectors, crystal lattice, unit cell (16 points)

1. Exercise on operations with vectors in crystallography (5 points)

The structure of quartz has the following lattice constants:

$$a = b = 4.9, c = 5.405 \text{ \AA}, \alpha = \beta = 90^\circ, \gamma = 120^\circ.$$

The positions of three atoms in the unit cell are given:

$$\text{Si: } [0.45, 0, 0.5]$$

$$\text{O}_1: [0.41, 0.26, 0.41]$$

$$\text{O}_2: [0.73, 0.14, 0.71]$$

Calculate the bond distances Si – O₁, Si – O₂ (in Å) and bond angles O₁ – Si – O₂ (in degrees), by using operation of dot product in crystallographic coordinate system.

2. Exercise on visualizing crystal structures (4 points)

The lattice constants of GaAs crystal are:

$$a = b = c = 5.65 \text{ \AA}, \alpha = \beta = \gamma = 90^\circ.$$

The unit cell is composed of 8 atoms, whose fractional positions are:

$$\text{Ga } [0, 0, 0], \text{Ga } [0 \frac{1}{2} \frac{1}{2}], \text{Ga } [\frac{1}{2} 0 \frac{1}{2}], \text{Ga } [\frac{1}{2} \frac{1}{2} 0]$$

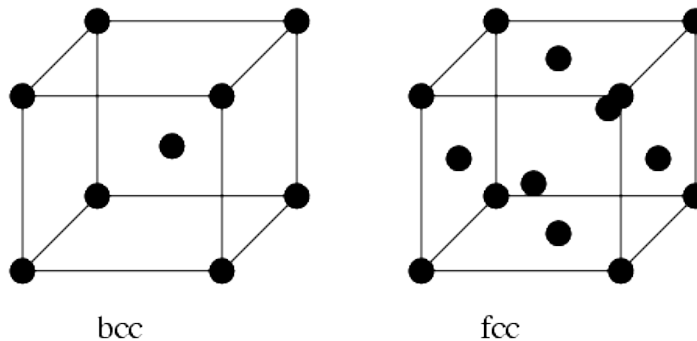
$$\text{As } [\frac{1}{4}, \frac{1}{4}, \frac{1}{4}], \text{As } [\frac{1}{4} \frac{3}{4} \frac{3}{4}], \text{As } [\frac{3}{4} \frac{1}{4} \frac{3}{4}], \text{As } [\frac{3}{4} \frac{3}{4} \frac{1}{4}].$$

1. Find the position of atoms inside a parallelepiped, containing 2 unit cells in each direction (8 crystallographic unit cells in total).

- Plot the resulting structure in projection along one of the crystallographic axis (**a**, **b** or **c**).

3. FCC and BCC structures of iron (4 points)

Fe crystallizes in two phases, face-centred cubic (FCC) and Body-centred cubic (BCC) phase.



- Calculate the packing density of both phases. Atoms can be approximates by a hard sphere shape with constant radius.
- Indicate the closest distance between two neighbour atoms in the FCC and BCC structure.
- Calculate the packing density defined as the ratio:

$$P = \text{Number}^{\text{sphere}} \frac{\text{Volume}^{\text{sphere}}}{\text{Volume}^{\text{unit cell}}}$$

4. Mass density of crystals from the structural data (3 points).



Calculate the mass density ($[g/cm^3]$) of GaAs material (structure is described in the task 1), diamond and graphite.

Please return on 28/10/2015