

Exercise for Solid State Physics for Nanoscience
SS 2019
Exercise sheet 4

4.1 Intrinsic Carrier concentration vs. Temperature

The density of free electrons n (holes p) is given below:

$$n = 2 \left(\frac{2\pi m_n kT}{h^2} \right)^{\frac{3}{2}} e^{-\frac{E_C - E_F}{kT}}; \quad p = 2 \left(\frac{2\pi m_p kT}{h^2} \right)^{\frac{3}{2}} e^{-\frac{E_F - E_V}{kT}}$$

E_C , E_V and E_F are the conduction, valance and Fermi energy levels. For intrinsic semiconductors the number of electrons is equal to the number of holes ($n=p=n_i$).

Scale the intrinsic carrier concentrations for germanium, silicon and GaAs from room temperature ($T = 300$ K) to 0 °C and liquid nitrogen temperature ($T = 77$ K) using the data below:

	Si	Ge	GaAs
E_G [eV]	1.12	0.67	1.35
$\frac{dE_G}{dT}$ [eV/K]	-2.3×10^{-4}	-3.7×10^{-4}	-5.0×10^{-4}
$n_i(300K)$ [cm^{-3}]	1.45×10^{10}	2.4×10^{13}	1.79×10^6

4.2 Space charge region of pn-Junction

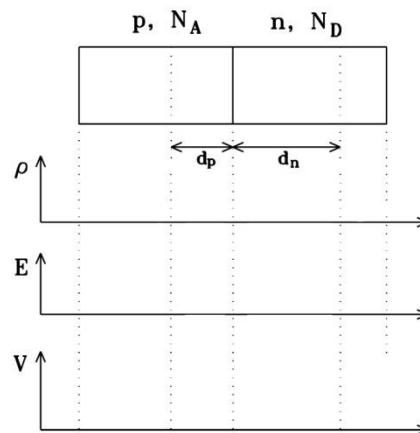
- Find the built-in voltage for a silicon p-n junction at room temperature with doping concentrations $N_A = 10^{16} \text{cm}^{-3}$ (acceptor) and $N_D = 10^{12} \text{cm}^{-3}$ (donor).
- Derive the width of the natural space-charge region and the maximum electric field ϵ_{\max} for an abrupt p-n junction as a function of the doping concentration N_A and N_D . Calculate the width for a very highly doped ($N_A=10^{16} \text{cm}^{-3}$) p-type junction on n-type detector-grade material with $N_D=10^{12} \text{cm}^{-3}$.

4.3 Structure of Bands

(a) Draw a pn diode junction in thermal equilibrium with its parts separated. Indicate on the sketch the levels of the valance band energy, conduction band and Fermi energy for both the p and n type semiconductors.

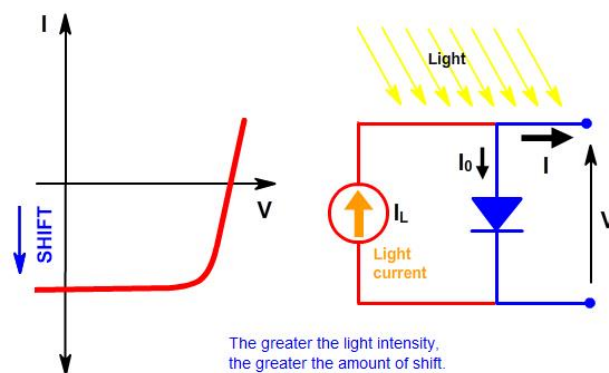
(b) Repeat part (a) when the two semiconductors are brought together.

(c) see 4.2b For different doping concentration of the p and n type materials, plot the change of the electric field E , the potential V and the charge density ρ along the depleted area. Use figure below.



Exercise 4: Solar Cell

A biased pn-junction is a basic element of silicon solar cells. Its function can be understood by means of the I-V characteristics curve of a pn-junction shifted by I_L along the current axis (towards





negative current), where I_L is the radiation induced current. Determine the effective working point (I_w, V_w) providing maximum power harvest of the solar cell. Neglect any other losses and suppose that V_{oc} is known (open circuit).